

$$3.10.2) \quad y'' - 2 \tan x y' = 0 \quad y' = p, \quad y'' = p' \Rightarrow p' - 2 \tan x p = 0 \Rightarrow \frac{dp}{dx} = 2 \tan x p \Rightarrow \frac{dp}{p} = 2 \tan x dx \Rightarrow \ln p = -2 \ln \cos x + \ln c \Rightarrow p = \frac{c}{\cos^2 x}$$

$$\Rightarrow \frac{dy}{dx} = \frac{c}{\cos^2 x} \Rightarrow dy = \frac{c}{\cos^2 x} dx \Rightarrow y_h = c_1 \tan x + c_2, \quad y_1 = \tan x, \quad y_2 = 1 \quad w(x) = \begin{vmatrix} \tan x & 1 \\ 1 + \tan^2 x & 0 \end{vmatrix} = -(1 + \tan^2 x)$$

$$y_p = -y_1 \int \frac{y_2 b(x)}{W(x)} dx + y_2 \int \frac{y_1 b(x)}{W(x)} dx \Rightarrow y_p = -\tan x \int \frac{(1)(1)}{-(1 + \tan^2 x)} dx + 1 \int \frac{\tan x (1)}{-(1 + \tan^2 x)} dx \Rightarrow y_p = \tan x \int \cos^2 x dx - \int \frac{\tan x}{1 + \tan^2 x} dx$$

$$4.10.2) \quad y_1 = e^x, \quad y_2 = e^{2x} \quad w(x) = \begin{vmatrix} e^x & e^{2x} \\ e^x & 2e^{2x} \end{vmatrix} = e^{3x} \quad y_p = -e^x \int \frac{e^{2x} \sin(e^x)}{e^{3x}} dx + e^{2x} \int \frac{e^x \sin(e^x)}{e^{3x}} dx$$