

$$\mathcal{L}\left\{\frac{1}{e^t} + \sqrt{t} - \sin^2 3t + \cosh t\right\} = \frac{1}{s+1} + \frac{\Gamma(\frac{3}{2})}{s^{\frac{3}{2}}} + \frac{1}{2}\left(\frac{1}{s} - \frac{s}{s^2+9}\right) + \frac{s}{s^2-1}$$

$$\sin^2 3t = \frac{1-\cos 6t}{2}, \quad \Gamma\left(\frac{3}{2}\right) = \frac{1}{2}\Gamma\left(\frac{1}{2}\right) = \frac{\sqrt{\pi}}{2} \qquad \Gamma\left(\frac{1}{2}\right) = \sqrt{\pi}, \qquad \Gamma(\alpha+1) = \alpha\Gamma(\alpha)$$

$$\mathcal{L}\{u_a(t)\} = \int_0^\infty e^{-st} u_a(t) dt = \int_0^a e^{-st} (0) dt + \int_a^\infty e^{-st} (1) dt = \frac{-1}{s} e^{-st}$$

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$$f(t) = \begin{cases} e^{-t} & 0 < t \leq 1 \\ \sin t & 1 < t < 3 \\ t^2 & t \geq 3 \end{cases} \qquad f(t) = e^{-t}(u_0(t) - u_1(t)) + \sin t(u_1(t) - u_3(t)) + t^2(u_3(t) - u_\infty(t)) = e^{-t}(1 - u_1(t)) + \sin t(u_1(t) - u_3(t)) + t^2 u_3(t)$$

$$\int_0^\infty e^{-st} \delta_a(t) dt = e^{-as}$$